

# Viscosity behaviour of weakly charged polymer-ion complexes comprising poly(vinyl alcohol) and Congo red

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The reduced viscosity,  $\eta_R$ , of poly(vinyl alcohol)-Congo red (PVA-CR) complexes in aqueous solution has some unique features, such as (1) an appearance of a maximum at a given PVA concentration ( $C_{PVA}$ ) and (2) a time evolution of  $\eta_R$ , but only in the regime where the maximum appears. These characteristic features of the viscosity behaviour are simulated by using the theory of Rice and Kirkwood which takes into account the electrostatic interaction in the reduced viscosity.

(Keywords: poly(vinyl alcohol); viscosity; polymer-ion complex)

## INTRODUCTION

Polymer-ion complexes have attracted wide interest due to their scientific and technological importance<sup>1,2</sup>. Most of these complexes can be easily formed by adding different types of ions to an aqueous polymer solution. For example, poly(vinyl alcohol) (PVA) is known as a polymer which is capable of complexation with borate ions<sup>3-9</sup>, cupric ions<sup>10</sup>, and various other inorganic species, such as titanate<sup>11</sup>, antimonate<sup>12</sup>, and vanadate<sup>13,14</sup> ions. The complexation process can be classified by two steps, namely mono-complexation and di-complexation. The mono-complexation stage, an attaching of an ion to a unit of a polymer chain, leads to a polyelectrolyte-type behaviour of the polymer chain. When another monomer unit of a polymer chain is complexed to the attached ion, di-complexation occurs and the complexed ion behaves as a crosslink. However, these complexations take place according to a delicate balance of the complexation equilibria. Therefore, the charged groups can be easily dissociated from the polymer chain by changing the ionic environment, resulting in a drastic change in the rheological properties of the polymer solution. For these reasons, these polymer-ion complexes exhibit various features in their rheological properties.

In a previous paper<sup>15</sup>, we reported a unique phase behaviour of the PVA-Congo red ion complexes, i.e. a re-entrant sol-gel-sol-gel transition, and discussed the origin of this behaviour. Congo red is a crosslinker of PVA aqueous solutions under either neutral or mild basic conditions. The viscosity of PVA-Congo red aqueous solutions had certain characteristic features, such as (1) an appearance of a maximum at a given PVA concentration ( $C_{PVA}$ ) and (2) a time evolution of  $\eta_R$ , but only in the limited regime where the maximum appears. These

phenomena were qualitatively explained using a model of intra- and intermolecular crosslink formation in conjunction with electrostatic interactions. This model was examined by analysing the structure factor for PVA-Congo red ion complexes, obtained by small-angle neutron and X-ray scattering, as functions of the PVA and CR concentrations<sup>16</sup>.

In this paper, we construct a viscosity function based on a theory which takes account of the electrostatic interaction, and discuss the role of attached ions on the viscosity behaviour, as well as the sol-gel phase behaviour in PVA-CR ion complex solutions.

## EXPERIMENTAL

### Materials

Resaponified poly(vinyl alcohol), having a viscosity-average degree of polymerization ( $DP$ ) = 1800, was supplied by Nippon Synthetic Chemical Industry Co. Ltd. Details of the sample characteristics are described elsewhere<sup>15</sup>. PVA and Congo red (CR) aqueous solutions were prepared by dissolving each component in deionized water. The required PVA and CR solutions were then mixed at 80°C and kept in a temperature controlled room at 20°C. PVA-borate complex solutions were also prepared in order to compare the rheological properties of the PVA-CR and PVA-borate complex systems. The PVA-borate complex was prepared by mixing PVA, boric acid and NaOH, where NaOH was added to ionize the boric acid<sup>6-8</sup>. The concentration of the NaOH solution was 0.167 M.

### Viscosity measurements

The viscosities of PVA-CR complex solutions were measured with a Ubbelohde capillary viscometer at 60 ± 0.05°C. The time required for the solution to pass

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the two menisci of the viscometer was recorded. A typical time taken for this was  $\sim 100$  s, and was very reproducible, with an error of  $\pm 0.1$  s in most of the cases. Therefore, the relative error was estimated to be  $\sim 0.1\%$ . The measurements were repeated at least three times and the times obtained were arithmetically averaged and then converted to the relative viscosity,  $\eta_{rel}$ , i.e. the ratio of the solution viscosity,  $\eta$ , and that of the solvent,  $\eta_0$ . Most of the experiments were carried out by diluting the polymer solution step by step, which is a typical procedure adopted in Ubbelohde capillary viscometry. In some cases, however, a viscosity thickening was observed during the repetition of the viscosity measurement. In such a case, each polymer solution was individually examined after ageing the solution in the Ubbelohde capillary viscometer at  $60^\circ\text{C}$ .

The relative viscosity,  $\eta_{rel}$ , was further converted to the reduced viscosity,  $\eta_R$ , via the specific viscosity  $\eta_{sp}$ , both of which are defined as follows:

$$\eta_{sp} = \eta_{rel} - 1 \quad (1)$$

and

$$\eta_R = \frac{\eta_{sp}}{C_{PVA}} \quad (2)$$

where  $C_{PVA}$  is the PVA concentration in monomeric units. Thus the intrinsic viscosity,  $[\eta]$ , can be described by the following:

$$\eta_R \rightarrow [\eta], \text{ for } C_{PVA} \rightarrow 0 \quad (3)$$

## RESULTS

### Electrostatic screening effects on viscosity

Figure 1 shows the variation of the reduced viscosity,  $\eta_R$ , for PVA aqueous solutions of PVA-CR and PVA-borate ion complexes. The abscissa is the crosslinker concentration,  $C_x$ , i.e. the CR or boric acid concentration. The PVA concentrations used were  $0.12$  and  $0.11 \text{ mol l}^{-1}$ , respectively, for the PVA-CR and PVA-borate complexes. Although these concentrations are smaller than the calculated chain overlap concentration,  $C_{PVA}^* \sim 0.55 \text{ mol l}^{-1}$  (ref. 15), it should be pointed out that we are examining here the crossover region from the dilute to the semidilute regimes because of the fact that the PVA chains are expected to be highly expanded owing to the attached ions. It should be noted that  $\eta_R$  for the PVA-CR ion complex is a stronger function of  $C_x$  than that of the PVA-borate complexes. In particular, for  $C_x > 0.012 \text{ mol l}^{-1}$ , a steep increase in  $\eta_R$  for the PVA-CR system is observed, which is in contrast to the  $C_x$  dependence of the PVA-borate complexes. We will discuss this point later.

### PVA concentration dependence

Figure 2 shows the variation of  $\eta_R$  as a function of  $C_{PVA}$  for various CR concentrations. In the case of  $C_{CR} = 0$ ,  $\eta_R$  behaves just as would be expected for a neutral polymer solution. The ordinate is taken with a logarithmic scale so as to stress the change in  $\eta_R$  at low  $C_{CR}$  values. By adding CR,  $\eta_R$  shows an upturn at low  $C_{PVA}$  values, typical of polyelectrolytes<sup>17,18</sup>. The higher the  $C_{CR}$ , then the higher the  $\eta_R$  at low  $C_{PVA}$  values. This clearly indicates that the higher the  $C_{CR}$ , then the higher is the concentra-

tion of the PVA-CR complexes. For  $C_{CR} \leq 0.003 \text{ mol l}^{-1}$ , most of the added CR ions seem to be attached to PVA chains and generate a repulsive interaction between the latter, where no significant electrostatic screening effect is observed in this concentration range. This kind of polyelectrolyte effect, an upturn behaviour in  $\eta_R$  at low  $C_x$  values, was not observed for the PVA-borate complexes, as shown in Figure 3 of ref. 8.

For larger  $C_{CR}$  values (i.e.  $C_{CR} \geq 0.015 \text{ mol l}^{-1}$ ),  $\eta_R$  starts to show a distinct maximum with increasing  $C_{CR}$  over the intermediate concentration range of PVA, i.e.  $0.05 \text{ mol l}^{-1} \leq C_{PVA} \leq 0.4 \text{ mol l}^{-1}$ . A time-dependent viscosity thickening was also observed exclusively in this concentration regime. The plots shown here are corresponding to equilibrium values of  $\eta_R$ , which were measured 4 days after loading the solution into the viscometer. For  $C_{PVA} > 0.4 \text{ mol l}^{-1}$ , however,  $\eta_R$  becomes insensitive to either  $C_{CR}$  or time, and the viscosity varies similarly to that of a PVA aqueous solution, i.e.  $C_{CR} = 0$ . The maximum value of  $\eta_R$  is about 10 to 40 times as high as that for the case with  $C_{CR} = 0$ , when compared at the same  $C_{PVA}$  value. It is worthwhile to note that the PVA concentration where  $\eta_R$  recovers a behaviour which is similar to that of the non-charged PVA solution, is roughly proportional to  $C_{CR}$ .

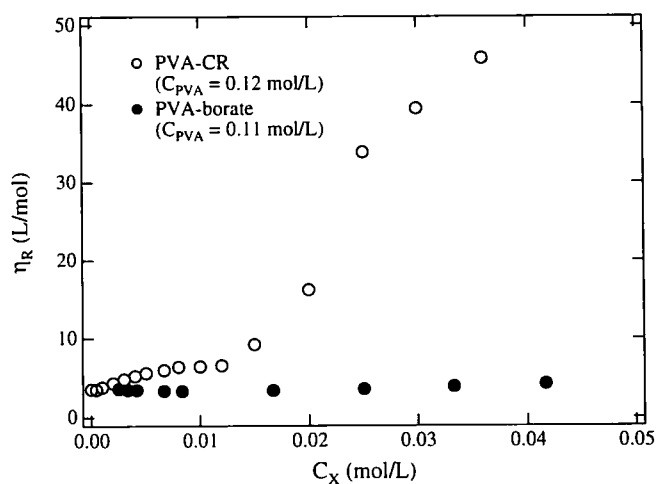


Figure 1 Crosslinker concentration ( $C_x$ ) dependence of the reduced viscosity,  $\eta_R$ : (●) boric acid; (○) Congo red

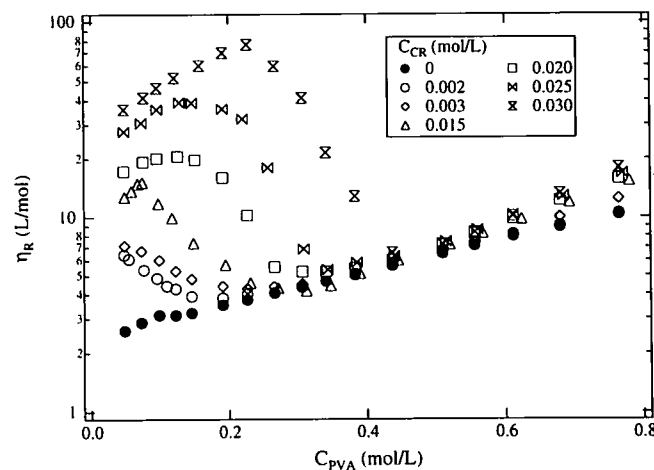
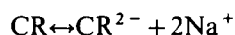


Figure 2  $C_{PVA}$  dependence of  $\eta_R$  for various concentrations of Congo red (CR)

## DISCUSSION

In this section, we shall try to explain the unique viscosity behaviour of the PVA-CR aqueous solutions described above. CR molecules dissociate into CR ions (abbreviated to  $\text{CR}^{2-}$ ) and  $\text{Na}^+$  ions in an aqueous solution as follows:



We assume here a 100% dissociation of the CR molecules under the conditions employed in this work. This assumption is supported by the fact that direct dyes, e.g. Congo red, are highly dissociated in aqueous solutions<sup>19</sup>. Therefore, the CR ion concentration,  $[\text{CR}^{2-}]$  can be regarded as being equal to  $C_{\text{CR}}$  without losing the essential points of the discussion.

## Electrostatic screening effects on viscosity

As was shown in Figure 1, a significant difference in the viscosity behaviours was observed between the PVA-borate and PVA-CR complexes at  $C_x > 0.015 \text{ mol l}^{-1}$ . Let us clarify the reason for this.

Figure 3 shows enlarged plots of Figure 1, where it should be noted that the ordinate is highly expanded. The slight discrepancy in the limiting value of  $\eta_R$  at  $C_x = 0$  is due to the presence of NaOH in the PVA-borate complexes. As shown in this figure,  $\eta_R$  for the PVA-borate complexes at first slightly decreases, and then increases with  $C_x$ . This interesting behaviour was also observed by Ochiai *et al.*<sup>4</sup> for the intrinsic viscosity,  $[\eta]$ , of PVA-borax aqueous solutions. According to the theory of Leibler *et al.*<sup>20</sup>, the initial concentration in  $[\eta]$  is due to the intrachain crosslinking via complexation of the PVA-borate ions. This kind of contraction was observed when a small amount of salt was added to the solution. The subsequent increase in  $[\eta]$  with increasing  $C_x$  was explained as being due to an electrostatic repulsion between the attached ions on the PVA chains. However, such a type of variation in  $\eta_R$  or  $[\eta]$ , i.e. a contraction and a gradual increase in  $\eta_R$ , was not observed for the PVA-CR system. The absence of a contraction in  $[\eta]$  at low  $C_x$  values for PVA-CR is explained as follows. Since there is no added salt in the case of PVA-CR, the addition of a small amount of CR ions leads to an expansion of the PVA chains. In the case of the PVA-borate complexes, the electrostatic repulsion between the

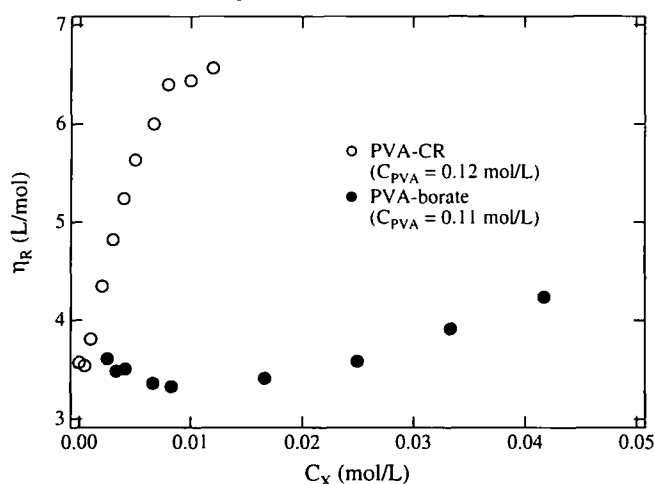


Figure 3 Crosslinker concentration,  $C_x$ , dependence of the reduced viscosity,  $\eta_R$ , at low  $C_x$  levels: (●) boric acid; (○) Congo red

attached ions is highly screened by the  $\text{Na}^+$  and  $\text{OH}^-$  ions introduced in order to ionize the boric acid. These ions behave as an added salt.

The spatial range of the electrostatic screening is given by the so-called Debye screening length,  $r_D$ , which is a function of the ionic strength,  $I$ , and the Bjerrum length,  $Q$ , as follows:

$$r_D = (8\pi N_A Q I)^{-0.5} \quad (4)$$

where

$$I = \frac{1}{2} \sum_i C_i z_i^2 \quad (5)$$

and

$$Q = \frac{e^2}{4\pi\epsilon k_B T} \quad (6)$$

where  $C_i$  and  $z_i$  are, respectively, the concentration and valency of the ion  $i$ .  $N_A$ ,  $e$ ,  $\epsilon$ , and  $k_B T$ , are the Avogadro constant, the elementary charge, the dielectric constant, and the Boltzmann energy, respectively. The value of  $r_D$  for the solution with borate ion ( $C_x = 0.01 \text{ mol l}^{-1}$ ) and NaOH (0.167 M) is calculated to be 7.3 Å at 25°C. On the other hand,  $r_D$  for the CR solution with  $C_x = 0.01 \text{ mol l}^{-1}$  is 18 Å; note that  $z$  is 2 for CR ions. Although these values are modified by complexation with PVA when these molecules are present in the solution, the estimated difference in  $r_D$  seems to be significant enough to change the viscosity behaviour at low  $C_x$  values (see Figure 3), which is ascribed to the addition of NaOH to the borate solution.

The steep increase in  $\eta_R$  for  $C_{\text{CR}} > 0.012 \text{ mol l}^{-1}$  in Figure 1 can be explained by using the same reasoning. When the number of attached CR ions is increased by increasing  $C_x$ , the repulsive electrostatic interaction increases as the quadratic power of  $C_x$ , according to the Coulomb law. In reality, the distance between charges should decrease with  $C_x$  because of a further attachment of CR ions to the PVA chains, thus giving rise to a higher power of  $C_x$  in the electrostatic potential. This may be the case for PVA-CR at  $C_x > 0.012 \text{ mol l}^{-1}$ . In the case of the PVA-borate ion complex with NaOH (0.167 M), the concentrations of  $\text{Na}^+$  and  $\text{OH}^-$  are of the order of  $10^{-1} \text{ mol l}^{-1}$ , which are at least ten times as high as the borate concentration. The experimental evidence shown above clearly indicates that the electrostatic interaction plays an important role in generating the unique rheological properties of the PVA-CR aqueous solutions.

## PVA concentration dependence

It is well known that the reduced viscosity,  $\eta_R$ , for polyelectrolyte solutions is considerably different from that of neutral polymer solutions at low polymer concentrations. This is empirically described by Fuoss<sup>17,18</sup> as follows:

$$\eta_R = \frac{A}{1 + BC^{0.5}} \quad (7)$$

where  $A$  and  $B$  are constants and  $C$  is the polymer concentration. Since equation (7) does not have any fundamental theoretical basis, theoretical investigations have been made by several workers, such as, Witten and Pincus<sup>21</sup>, Rabin<sup>22</sup>, Borsali *et al.*<sup>23</sup>, and Nishida *et al.*<sup>24</sup>.

These theories predict that  $\eta_R$  has a maximum,  $\eta_{R,\max}$  at  $C_{\max}$ , in the plot of  $\eta_R$  versus  $C$ , and that  $\eta_{R,\max}$  becomes higher and  $C_{\max}$  moves to a lower concentration by increasing the charge density on the polymer or by decreasing the salt concentration<sup>23</sup>. Our results for the  $C_x$  dependence of  $\eta_{R,\max}$  are opposite to that predicted by the theories, i.e.  $\eta_{R,\max}$  moves to a larger  $C_{PVA}$  with increasing  $C_{CR}$ . This contradiction may be accounted for by the ion complexation equilibrium between PVA and CR.

Now we shall try to reproduce the  $\eta_R$  variation as a function of  $C_{PVA}$ , based on the Rice and Kirkwood (RK) theory<sup>25</sup>. Although the RK theory itself does not take account of the polymer effect, it provides a clear physical picture of the electrostatic interaction between charges when compared with more sophisticated theories<sup>21-23</sup>. Therefore, we will use the RK theory, as employed by Nishida *et al.*<sup>24</sup>, so as to stress the contribution of the electrostatic interaction of the attached charges on a polymer chain. The polymer effect will be incorporated by introducing the radial distribution function of the attached ions for a charged polymer chain. According to the theory, the contribution of the electrostatic interaction between charges to the reduced viscosity,  $\eta_{R,\text{ion}}$ , is given by the following:

$$\eta_{R,\text{ion}} \approx C^2 \int_{r_0}^{\infty} r^2 \left[ u''(r) + \frac{4u'(r)}{r} \right] g(r) 4\pi r^2 dr \quad (8)$$

where  $r_0$  is the lower cutoff and  $u'(r)$  and  $u''(r)$  are the first and second derivatives, respectively, of the electrostatic potential,  $u(r)$ , which is itself given by the following<sup>20</sup>:

$$\frac{u(r)}{k_B T} = \frac{(ze)^2}{4\pi\epsilon r k_B T} \exp\left(-\frac{r}{r_D}\right) = \frac{z^2 Q}{r} \exp\left(-\frac{r}{r_D}\right) \quad (9)$$

where  $z$  is the valence number of the polyion, and  $r_D$  is the Debye length, as defined in equation (4). In addition,  $g(r)$  is the radial distribution function of the polyion and is given for a dilute polymer solution as follows<sup>26</sup>:

$$g(r) = \exp\left(-\frac{u(r)}{k_B T}\right) \quad (10)$$

When  $u(r) \ll k_B T$ , equation (10) can be truncated to:

$$g(r) \approx 1 - \frac{u(r)}{k_B T} \quad (11)$$

This enables one to perform the analytical integration of equation (8), which gives the following:

$$\eta_{R,\text{ion}} \approx C^2 \left[ z^2 Q \left( \frac{r_0^3}{r_D} + r_0^2 \right) \exp\left(-\frac{r_0}{r_D}\right) + z^4 Q^2 \left( -\frac{r_0^2}{2r_D} + \frac{r_0}{2} + \frac{5r_D}{4} \right) \exp\left(-\frac{2r_0}{r_D}\right) \right] \quad (12)$$

The assumption made in the derivation of equation (12) was confirmed as being relevant as long as we set an appropriate value for  $r_0$  in the process of the integration of equation (8). So now we can estimate  $r_0$ , the distance between the neighbouring charges on the chain, based on the discussion by Leibler *et al.* for PVA-borate ion complexes<sup>20</sup>. Thus,  $r_0$  is given by the following:

$$r_0 = b_{PVA} \sqrt{n} \quad (13)$$

where  $b_{PVA} (= 6.3 \text{ \AA})^{27}$  is the segment length of the PVA chain and  $n$  is the number of monomers between successive attached ions on a chain. The latter is given by:

$$n = \frac{1 + \tilde{K} C'_{CR}}{\tilde{K} C'_{CR}} \quad (14)$$

where  $\tilde{K}$  is the effective complexation constant, given as follows:

$$\tilde{K} = K \exp\left(-\frac{\alpha u(r=r_0)}{k_B T}\right) \quad (15)$$

This implies that the effective complexation constant is suppressed by the presence of an electrostatic potential. In equation (15),  $\alpha$  is a numerical factor, which is fixed at  $4^{20}$ ,  $u(r=r_0)$  is the electrostatic interaction energy between charges separated by  $r_0$ , and  $C'_{CR}$  is the concentration of free CR ions. Since  $C'_{CR}$  is a decreasing function of  $C_{PVA}$ , we assume the following functional forms for  $C'_{CR}$ :

$$C'_{CR} = C_{CR} - \frac{1}{20} C_{PVA}, \quad \text{for } C_{CR} > \frac{C_{PVA}}{20} \quad (16a)$$

and

$$C'_{CR} = 0, \quad \text{for } C_{CR} \leq \frac{C_{PVA}}{20} \quad (16b)$$

The numerical factor,  $1/20$ , is based on the results obtained by Fujino and Fujimoto<sup>28</sup>. This indicates that CR molecules are attached to every 20 monomer units of the PVA chains, at most. The complexation constant,  $K$ , in the absence of any electrostatic interaction, is estimated to be  $11 \text{ mol}^{-1}$  for PVA-borate ion complexes<sup>20</sup>. We shall employ this value here in order to simulate the reduced viscosity variation with  $C_{PVA}$ .

The variations of  $\eta_{R,\text{ion}}$  versus  $C_{PVA}$ , for  $C_{CR} = 0.015, 0.020, 0.025,$  and  $0.030 \text{ mol l}^{-1}$  are shown in Figure 4. The general trend of  $\eta_{R,\text{ion}}$  well reproduces the observed reduced viscosity curves for  $C_{PVA} \leq 0.4 \text{ mol l}^{-1}$ , which indicates that  $\eta_{\text{ion}}$  contributes significantly to the net viscosity. In fact,  $\eta_{R,\text{ion}}$  does have a maximum at around  $C_{PVA} = 0.02 \text{ mol l}^{-1}$ , which shifts to higher concentrations

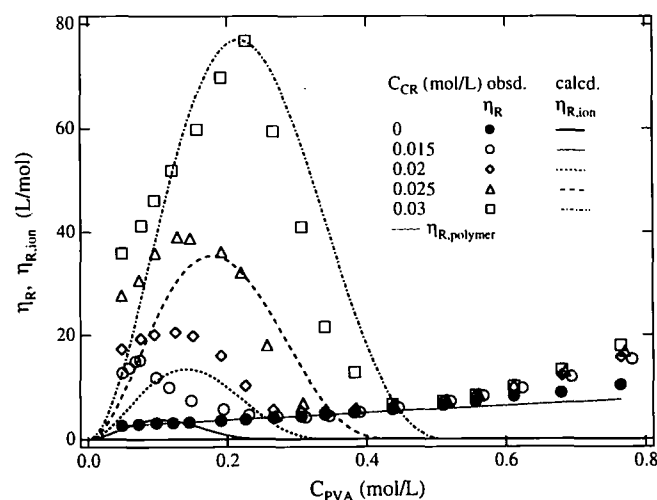


Figure 4 Theoretical calculations of the contribution of the electrostatic interaction to the reduced viscosity,  $\eta_{R,\text{ion}}$ , for  $C_{CR} = 0.015, 0.020, 0.025,$  and  $0.030 \text{ mol l}^{-1}$ , as a function of  $C_{PVA}$ . The theoretical curves were scaled in order to adjust the maximum of the observed  $\eta_R$  for  $C_{CR} = 0.030 \text{ mol l}^{-1}$ .

by increasing  $C_{CR}$ . Since the RK theory does not take account of the viscosity increase due to the presence of polymer chains, the net reduced viscosity,  $\eta_R$ , for a weakly charged polymer solution should be given by the following:

$$\eta_R = \eta_{R,\text{polymer}} + \eta_{R,\text{ion}} \quad (17)$$

where  $\eta_{R,\text{polymer}}$  is the reduced viscosity for a non-charged polymer solution. In addition,  $\eta_{R,\text{polymer}}$  is a function of the polymer concentration,  $C$ , according to the following well known relationship:

$$\eta_{R,\text{polymer}} = [\eta] + k'[\eta]^2 C \quad (18)$$

where  $k'$  is the Huggins constant<sup>29</sup>. The value of  $k'$  is known to be an invariant with respect to the temperature and the nature of the solvent. The values of  $[\eta]$  and  $k'$  for a solution of PVA ( $DP=1800$ ) at  $60^\circ\text{C}$  were estimated to be  $2.301\text{mol}^{-1}$  and  $1.30$ , respectively, for  $C_{PVA} \leq 0.38\text{mol l}^{-1}$ . These values are comparable to those obtained by Tager *et al.* ( $[\eta]=3.61\text{mol}^{-1}$  and  $k'=1.32$  for an aqueous solution of PVA ( $DP \approx 1050$ ) at  $50^\circ\text{C}$ )<sup>30</sup>. It is obvious that the deviation of the observed  $\eta_R$  from  $\eta_{R,\text{ion}}$  results from the presence of  $\eta_{R,\text{polymer}}$ .

Figure 4 clearly indicates that the viscosities of the polymer solutions are drastically changed by the introduction of attached ions to the polymer. This  $C_{CR}$  dependence of the maximum in  $\eta_{R,\text{ion}}$  is opposite to the general trend observed for polyelectrolytes<sup>24</sup>. We should remind ourselves here that the attached charge density for the PVA-CR complexes is a function of  $C_{CR}$  and  $C(=C_{PVA})$ , which is given by equations (13)–(16b), because it is determined by the complexation equilibrium. On the other hand, the degree of ionization for typical polyelectrolytes is invariant as far as a full ionization is attained. This essential difference results in the opposite dependence of the position and the height of  $\eta_{R,\text{max}}$  on the charge density concentration, i.e.  $C_{CR}$  in the case of PVA-CR. At higher PVA concentrations,  $\eta_{R,\text{ion}}$  becomes zero, recovering the same value of  $\eta_R$  as that of non-charged PVA solutions, i.e.  $\eta_{R,\text{polymer}}$ .

#### Time evolution of the reduced viscosity

As indicated above,  $\eta_R$  increases only over the limited region where a maximum appears in the  $\eta_R$  versus  $C_{PVA}$  plots. Figure 5 shows plots of the time evolution of  $\eta_R$ . The solid curves are the ones fitted by using an exponential-type function, which is given by the following:

$$\eta_R(t) = (\eta_R^\infty - \eta_R^0)[1 - \exp(-t/\tau)] + \eta_R^0 \quad (19)$$

where  $\eta_R^0$  and  $\eta_R^\infty$  are the reduced viscosities at time  $t=0$  and  $t=\infty$ , respectively, and  $\tau$  is the viscosity thickening half-time. Equation (19) indicates that additional cross-links are formed by ageing at a constant rate of  $1/\tau$ , as follows:

$$\frac{d}{dt} \left[ \frac{\eta_R(t) - \eta_R^0}{\eta_R^\infty - \eta_R^0} \right] = \frac{1}{\tau} \quad (20)$$

The observed data points can be reproduced by using equation (19) except for the low- $t$  region where a different viscosity thickening mechanism may be present.

Figure 6 shows the variation of  $\eta_R^0$ ,  $\eta_R^\infty$ , and  $\tau$  with  $C_{CR}$ . The dashed line indicates the value of  $\eta_R$  for a non-charged PVA solution having the same  $C_{PVA}$ . Since  $\tau$  is more or less constant ( $\sim 27$  h), irrespective of  $C_{CR}$ , the

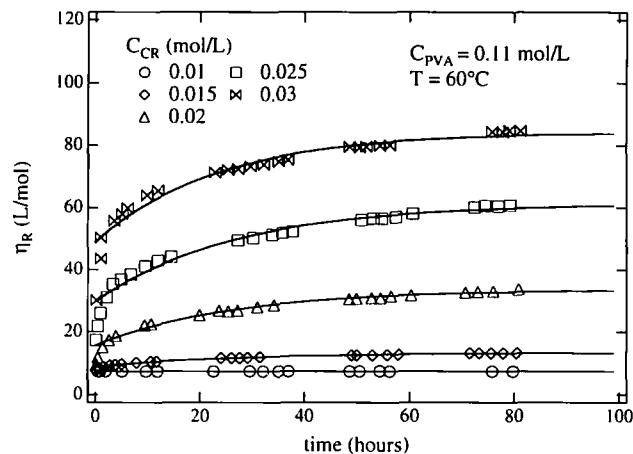


Figure 5 Time evolution of  $\eta_R$  for PVA-CR ion complex solutions with different values of  $C_{CR}$ ; the continuous curves are fitted using equation (19)

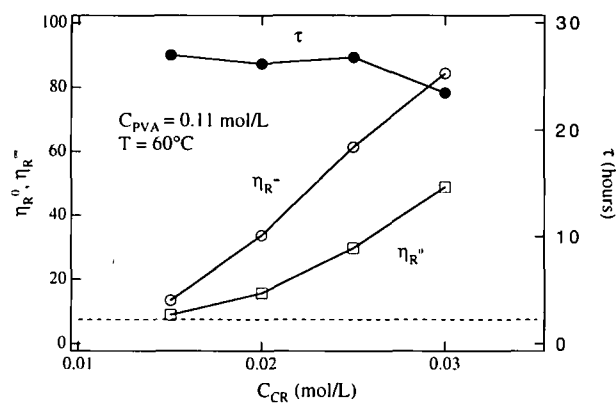


Figure 6  $C_{CR}$  dependence of  $\eta_R^0$ ,  $\eta_R^\infty$ , and  $\tau$ ; the dashed line indicates  $\eta_R$  for a non-charged PVA solution

viscosity thickening mechanism does not change in the concentration region where  $C_{CR} \geq 0.015\text{mol l}^{-1}$ . However,  $\eta_R^0$  and  $\eta_R^\infty$  both increase linearly with  $C_{CR}$  in the same  $C_{CR}$  region. This experimental evidence indicates that there exists a lower limit of  $C_{CR}$  where time-dependent viscosity thickening takes place. Viscosity thickening with time is usually explained by the occurrence of a successive hydrogen bonding process, for example in the case of the PVA-vanadate ion complexes<sup>14</sup>. However, in the case of the PVA-CR ion complexes, a viscosity thickening was observed at  $60^\circ\text{C}$ , where hydrogen bonds are believed to be absent. In addition, the good agreement between the observed and calculated viscosity behaviour shown in Figure 4 suggests that the unique behaviour of  $\eta_R$  for the PVA-CR system can be interpreted without introducing the idea of hydrogen bonds. As has been discussed in ref. 15, the CR molecules themselves have a capability for undergoing viscosity thickening via (1) hydrogen bonding, (2) association of azo and amino groups, and/or (3) stacking of naphthalene groups. At a relatively high temperature, such as  $60^\circ\text{C}$ , the association and/or stacking seem to be more favourable, resulting in a slow viscosity thickening. This interpretation does not contradict the assumption made in the theoretical calculation.

## CONCLUSIONS

The viscosities of PVA-CR ion complexes in aqueous

solutions were measured as functions of the PVA ( $C_{\text{PVA}}$ ) and CR ( $C_{\text{CR}}$ ) concentrations. A comparison of the crosslinker concentration dependence of the reduced viscosity,  $\eta_{\text{R}}$ , between the PVA-CR and PVA-borate complexes indicated the presence of strong electrostatic repulsive interactions in the PVA-CR complexes.

The  $C_{\text{PVA}}$  dependence of  $\eta_{\text{R}}$  showed some interesting features, namely (1) the appearance of a maximum at a given PVA concentration ( $C_{\text{PVA}}$ ) and (2) a time evolution of  $\eta_{\text{R}}$ , but only in the regime where the maximum appears. For low values of  $C_{\text{CR}}$ , the behaviour of the reduced viscosity,  $\eta_{\text{R}}$ , is very similar to that observed for polyelectrolyte solutions without salt. However, for the high  $C_{\text{CR}}$  regime, the  $C_{\text{PVA}}$  dependence of  $\eta_{\text{R}}$  has a distinct maximum, with this maximum becoming higher with increasing  $C_{\text{CR}}$ . Although this tendency is similar to that observed for polyelectrolytes, the fact that the maximum moves in the direction of higher  $C_{\text{PVA}}$  values with increasing  $C_{\text{CR}}$  is opposite to the typical polyelectrolyte behaviour. These experimental findings were interpreted by using theoretical calculations of the electrostatic effect on the viscosity. The viscosity thickening could be fitted with an exponential-type function, which had a half-time  $\tau$  of  $\sim 27$  h, irrespective of  $C_{\text{CR}}$ .

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